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A Fast Method for Estimating Statistical Power of Multivariate GWAS in Real Case Scenarios: Examples from the Field of Imaging Genetics

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Abstract

In GWAS of imaging phenotypes (e.g., by the ENIGMA and CHARGE consortia), the growing number of phenotypes considered presents a statistical challenge that other fields are not experiencing (e.g. psychiatry and the Psychiatric Genetics Consortium). However, the multivariate nature of MRI measurements may also be an advantage as many of the MRI phenotypes are correlated and multivariate methods could be considered. Here, we compared the statistical power of a multivariate GWAS versus the current univariate approach, which consists of multiple univariate analyses. To do so, we used results from twin models to estimate pertinent vectors of SNP effect sizes on brain imaging phenotypes, as well as the residual correlation matrices, necessary to estimate analytically the statistical power. We showed that for subcortical structure volumes and hippocampal subfields, a multivariate GWAS yields similar statistical power to the current univariate approach. Our analytical approach is as accurate but ~ 1000 times faster than simulations and we have released the code to facilitate the investigation of other scenarios, may they be outside the field of imaging genetics.

Keywords Twin models · Statistical power · Multivariate · Univariate · GWAS · MRI imaging

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Introduction

The ENIGMA and CHARGE initiatives have been outstanding in uniting researchers from all over the world to perform large scale GWAS and identifying genetic variants contributing to head size (intracranial volume, ICV) and volumes of subcortical structures (Thompson et al. 2014). The sample size reached since the consortia began makes them the most powerful meta-analytic samples to study the genetics of the brain [see (Strike et al. 2015) for a review]. For example, the ENIGMA sample grew from ~8 k scans in the first GWAS on ICV

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and hippocampal volume (Stein et al. 2012), to ~40 k in the most recent analyses (combined with CHARGE and UK biobank) (Hibar et al. 2015; Adams et al. 2016) and we can expect the sample size to increase again in future analyses with a greater contribution from the biobanks (e.g. UK (Miller et al. 2016) and German biobanks (Greiser et al. 2014; Schram et al. 2014; Breteler et al. 2014). At the same time, the number of phenotypes considered has also increased (from 2 to 7 subcortical volumes to 68 cortical measurements) and we can expect even more phenotypes to be included in future projects (e.g. DTI or voxel-wise cortical morphology).

This raises the question of statistical power of GWAS analyses of magnetic resonance imaging (MRI) derived phenotypes, as the number of tests increases quickly. This led us to compare the statistical power of univariate and multivariate GWAS using realistic scenarios, to illustrate the potential and limitations of each approach.

Multivariate GWAS analyses often consist of a series of MANOVAs, which results in only one test of association per SNP, over all outcome variables considered. Such tests have been implemented in popular GWAS software such as PLINK (Ferreira and Purcell 2009; Purcell et al. 2007). Other multivariate approaches include MultiPhen (O'Reilly et al. 2012) that uses likelihood ratio test, and GEMMA, which further allows the modelling of participant relatedness (Zhou and Stephens 2014). In addition, Bayesian methods are available (Marchini et al. 2007; Stephens 2013), but controlling for familial or cryptic relatedness in these models may not be straightforward. Finally, Medland et al., (Medland and Neale 2010) proposed an integrated model that allows testing SNP effects on the common factor as well as on variable-specific factors, but it remains unclear which factors to test and how to handle the correction for multiple testing. The statistical power of the different multivariate approaches (see Supplementary Section 1 for a quick review) depends on the covariance structure of the phenotypes (van der Sluis et al. 2013; Galesloot et al. 2014; Cole et al. 1994; Minica et al. 2010), and, as nicely summarised by Zhou and Stephens (2014): "[...] in a GWAS setting, no single test will be the most powerful in detecting the many different types of genetic effects that could occur. It is possible to manufacture simulations so that any given test is most powerful".

Here, we aimed to calculate the statistical power of real-case multivariate GWAS of brain phenotypes, by integrating genetic and environmental correlations estimated from twin data. We chose to focus on MANOVA models as they are the direct multivariate equivalent of the univariate GWAS approach. In addition, unlike any other multivariate method, we can calculate the power analytically and avoid time-consuming simulations (Muller and Peterson 1984).

Materials and methods

MANOVA power calculation

Power calculation of multivariate linear models such as MANOVA may be seen as an extension of the power calculation in the univariate case (Muller and Peterson 1984). However, unlike the univariate case, we can choose between four test statistics: Roy's largest root (RLR), Hotelling-Lawley trace (HLT), Wilks' lambda (WL) [implemented in PLINK (Ferreira and Purcell 2009)] and Pillai-Bartlett trace (PB). We focused on the last three as they show the highest sensitivity (Olson 1974, 1976, 1979; Stevens 1979, 1980; Pillai and Jayachandran 1967) and can be well approximated by an F-distribution (Muller and Peterson 1984; Pillai 1956; Nagarsenker and Suniaga 1983; Rao 1973). Multivariate power calculations require specification of the sample size (N), design (X, SNP) and covariates, the vector of effect sizes (β, effects of SNP on phenotypes) and a matrix of residual variance–covariance of the phenotypes (Σ , "residual" means here that the SNP effect has been removed) (Muller and Peterson 1984). From there, power can be estimated using non-central F-approximation whose degrees of freedom depend on the choice of test-statistic (Muller and Peterson 1984).

To obtain realistic β and Σ for the set of brain phenotypes considered, we used a Cholesky decomposition of a multivariate twin model (Fig. 1). This is arguably one of the most general multivariate models and allows

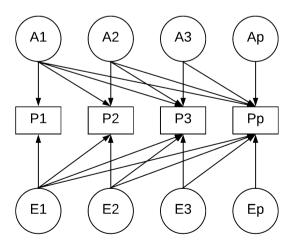


Fig. 1 General Cholesky decomposition of the genetic and environmental variance of the brain phenotypes. The *p* phenotypes are labels, P1 ... Pp; we also model additive genetic (A) and environmental (E) sources of variance, with latent variables, A1 ... Ap, E1 ... Ep. In this model, all of the genetic variance is accounted for by the p additive genetic latent factors and the SNP can only affect one of the independent genetic factors (here, A2). All of the genetic and environmental factors are independent



as many independent genetic or environmental factors as phenotypes, while minimising the number of paths. In this model, all the genetic variance is accounted for by the p additive genetic latent factors and the SNP can only affect one of the independent genetic factors (e.g. Fig. 1). Using a twin sample, we can estimate the matrices of path coefficients a and e that describe the relationship between latent variables A, E and phenotypes P:

$$P = aA + eE. (1)$$

In the example below (Fig. 1), the SNP affects the latent factor A2: A2 = $b \times \text{SNP} + \varepsilon$. Thus, our vector of effect size can be written as:

$$\beta = (0, b \times a_{22}, b \times a_{23}, \dots, b \times a_{2p})$$
 (2)

with $a_2 = (a_{22} \dots a_{2p})$ the path coefficients of the factor A2, estimated from the twin model, where SNP is the categorical variable of the observed genotype at a particular locus (e.g., 0: genotype aa, 1: aA, 2: AA). We can then choose b based on the maximum path coefficient and the SNP minor allele frequency (MAF) so that we express the power as a function of maximal phenotypic variance explained (R^2) by the SNP, independently of the SNP MAF. For example, if a_{23} is the largest path coefficient (in absolute value) and we set that the SNP explains at most R^2 of the variance of one trait, we can use:

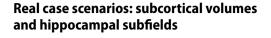
$$b = \frac{\sqrt{R^2}}{\text{SD (SNP)} \times a_{23}}$$
 (3)

with SD(SNP) = $\sqrt{2\text{MAF}(1-\text{MAF})}$, and a_{23} the standardised path coefficient. Specifying the SNP effect size in terms of R^2 (variance explained) simplifies the analysis as it integrates the effect size b and the SNP MAF. Finally, we can calculate the residual phenotypic variance—covariance matrix Σ , using the path coefficients from which we have subtracted the SNP effect. We used the fact that $\text{cov}(P) = a \times \text{t}(a) + e \times \text{t}(e)$ and that the phenotypic variance—covariance due to the SNP effect is $\text{cov}\left(P_{\text{SNP}}\right) = \frac{\sqrt{R^2}}{a_{23}} \times \text{t}(a_2) \times a_2$. Thus, the residual variance—covariance due to the sidual variance due to the sidual variance.

ance-covariance matrix of phenotypes (after removing the SNP effect) is

$$cov (P_{-SNP}) = a \times t(a) + e \times t(e) - cov (P_{SNP})$$
 (4)

As the estimated β and Σ are specific to the genetic additive factor on which the SNP loads (Fig. 1), we have to calculate the statistical power for each genetic factor. As the genetic factors are independent we aggregated the factor-specific power by taking the mean or the weighted mean (using the % of variance explained by each genetic factor as weights).



First, we considered seven subcortical volumes (summed over left and right hemisphere structures) processed using FreeSurfer 5.3 (Fischl 2012) using the ENIGMA protocols and QC (http://enigma.ini.usc.edu/protocols/imaging-protocols/). Then, we analysed volumetric data from 12 hippocampal subfields segmented using FreeSurfer 6.0 (Iglesias et al. 2015).

We fitted multivariate twin models with Cholesky decomposition in OpenMx (Boker et al. 2011) and extracted the standardised path coefficients to calculate the multivariate power. We calculated the power varying the sample size (up to N = 60,000) and the maximal SNP effect size (0.05–1% of variance explained).

For the univariate approach, we used a significance threshold of 5e–8/neff for univariate GWAS, with neff being the number of effectively independent phenotypes (Li and Ji 2005; Li et al. 2012), (code available at http://neurogenetics.qimrberghofer.edu.au/matSpDlite/). Such an approach has been used in prior MRI GWAS (Hibar et al. 2015) to ensure a FWER < 5% without over-correcting when performing tests over correlated variables. Here, we estimated neff to be six for the seven subcortical volumes (significance threshold of 8.3e–9) and 7 for the 12 hippocampal subfields (significance threshold of 7.1e–9), after regressing out all of the covariates (including ICV). For MANOVA power, we used the standard genome wide significance threshold for European populations (5e–8).

Multivariate twin modelling

We included 424 complete twin pairs (178 MZ, 246 DZ) with available volumes for the subcortical structures and hippocampal subfields. Participants included a slightly higher proportion of females (63.0%) and were on average 21.9 years old at scanning (SD=3.3, range 15–29). Missingness (after QC) was less than 1% in all the variables considered.

T1 weighted structural scans were collected as part of the QTIM study (de Zubicaray et al. 2008), with TR = 1500 ms, TE = 3.35 ms, TI = 700 ms, flip angle = 8° , 256 or 240 (coronal or sagittal) slices, FOV = 240 mm, $256 \times 256 \times 256$ (or $256 \times 256 \times 240$) matrix, slice thickness = 0.9 mm and voxel size 0.9 mm³.

Prior to twin modelling, age, age², age³, sex, acquisition direction (coronal/sagittal), and ICV were regressed from the subcortical and hippocampal subfield volumes, and we used the residuals in the following analyses. Multivariate twin models were run in OpenMx (Boker et al. 2011) using Full Information Maximum Likelihood, which allows for missing observations.



Supplementary Tables 1 and 2 report the estimated standardised path coefficients used in the power calculation. Using the path coefficients, one can calculate genetic and environmental correlations between the subcortical volumes or hippocampal subfields (Figs. 2, 3). The subcortical volumes and hippocampal subfields are genetically correlated (rG values between 0.10 and 0.54 for subcortical volumes, -0.22 and 0.86 for hippocampal subfields); this supports considering them in multivariate GWAS. In addition, the path coefficients indicate multiple independent sources of additive variance (large path coefficients outside of the first genetic factor), which suggests that a GWAS of the first PC would not capture all of the relevant information. These results are consistent with the genetic correlations previously reported (Renteria et al. 2014), even if our estimates are systematically lower, which we attribute to controlling for ICV.

Sensitivity of power calculation

In our power calculation, we used estimated parameters (path coefficients), which asks about the robustness of our results across the range of plausible path coefficients. We performed sensitivity analyses, varying the path coefficients in our power calculations to reflect the uncertainty

in the estimation. Thus, we randomly drew path coefficients values from their 95% confidence intervals and evaluated the impact of the new coefficients on our power calculation. We repeated this operation 100 times for each effect size, and visualised the uncertainty in power that results from the uncertainty in path coefficients. In addition, we checked if the power calculation remained the same after changing the order of the variables in the OpenMx model.

Next, we checked our analytical results against simulated statistical power, for the two main scenarios considered. We expect highly similar estimates of power as the F approximations used in the analytical approach should be accurate (Muller and Peterson 1984). In addition, we checked that MANOVA power in the particular case of a single phenotype was equivalent to those from a univariate model. Finally, we reported the computing time required for simulations in comparison to our analytical approach.

Fig. 2 Genetic (above diagonal) and environmental (below) correlations between subcortical volumes. Colour and size of the coloured squares indicate the strength of the correlations. No thresholding was applied to the matrix based on significance or correlation strength

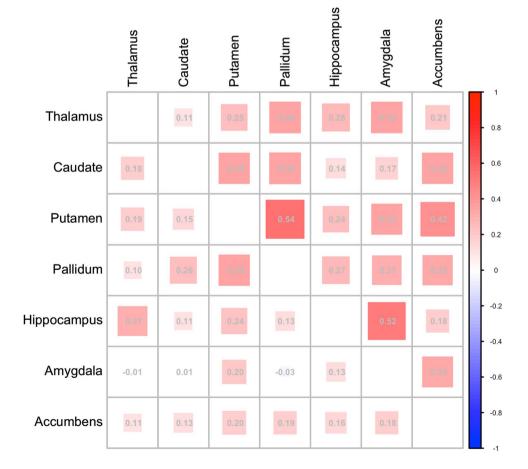
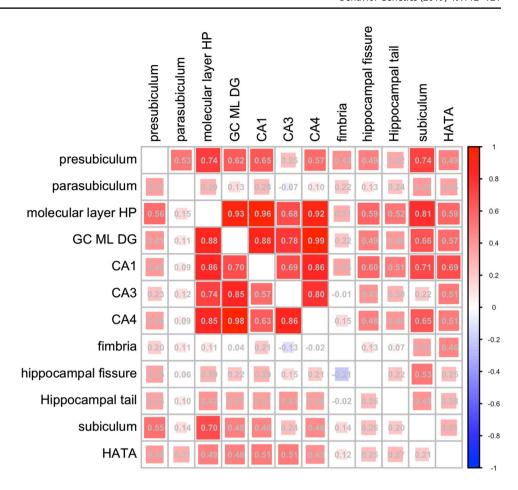




Fig. 3 Genetic (above diagonal) and environmental (below) correlations between hippocampus subfields. Colour and size of the coloured squares indicate the strength of the correlation. No thresholding was applied to the matrix based on significance or correlation strength. GC_ ML_DG: Granule Cells of the Molecular Layer of the Dentate Gyrus. CA1-4: Cornu Ammonis areas 1-4. CA2 and CA3 are merged, as FreeSurfer 6.0 does not differentiate between them (Iglesias et al. 2015). HATA: Hippocampus-amygdala transition area



Results

Multivariate versus univariate power

The statistical power of subcortical GWAS approaches is summarised in Fig. 4. The multivariate approach should be comparable or even slightly less powerful in identifying genome-wide significant variants. For example, the current ENIGMA sample (N \sim 30,000) would detect an association approximately four out of ten times (power = 0.38) with the univariate approach (for a SNP explaining 0.1% of the variance in any subcortical volume). For the same parameters, a multivariate approach should detect the association approximately three out of ten times. In other words, 80% statistical power would be achieved for a sample size of 48,000 in a multivariate analysis, compared to 43,000 in the univariate case.

Similarly, multivariate GWAS should lead to similar statistical power than the univariate approach using hippocampal subfields (Fig. 5). For a SNP explaining 0.1% of the variance in the volume of one of the subfields, 80% power can be achieved with a sample of 46,000 using multivariate GWAS, against 44,000 in the univariate case. The choice of test statistic (HLT, WL or PB) did not impact the power

calculation, consistent with prior research highlighting their equivalence in large samples (for $N > 10 \times p$, with p the number of dependent variables) (Muller and Peterson 1984).

The different weighting of factor-wise power in the multivariate calculation resulted in similar conclusions for the subcortical volumes scenario (Supplementary Figs. 1, 2). However, for the hippocampal subfields, the power of each genetic factor varied greatly and the multivariate power depended on the weights used to combine the factors (Fig. 6, Supplementary Figs. 3, 4, 5). Thus, the MANOVA does worse than in the univariate approach at detecting SNPs associated with the first additive genetic factor, but may provide more powerful at identifying SNPs influencing only a subset of hippocampus subfields (Fig. 6, Supplementary Fig. 5).

Sensitivity analysis

To evaluate the effect of uncertainty around path estimates on our power calculation, we re-ran the analysis 100 times randomly drawing path coefficients from their 95% confidence intervals. Variations in path coefficients resulted in small variations of multivariate power, over a hundred iterations (Supplementary Figs. 6, 7), with no consequences on



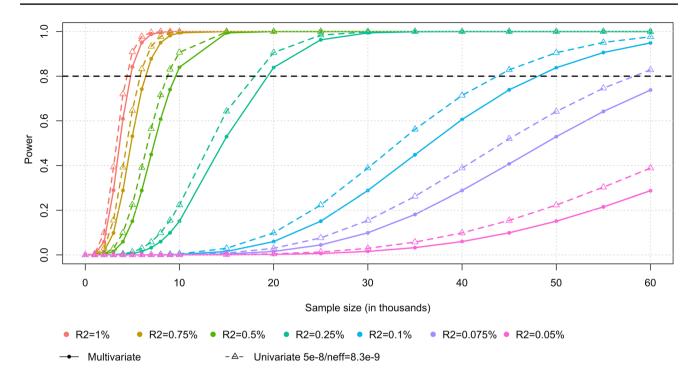


Fig. 4 Statistical power as a function of sample size for multivariate (solid lines) and univariate (dashed/dotted lines) GWAS on subcortical volumes. For all effect sizes and sample sizes, the multivariate approach confers greater statistical power than univariate approach.

Multivariate power presented here corresponds to the varianceweighted power of genetic factor. Simply averaging the power across all factors did not change the conclusions (Supplementary Fig. 1)

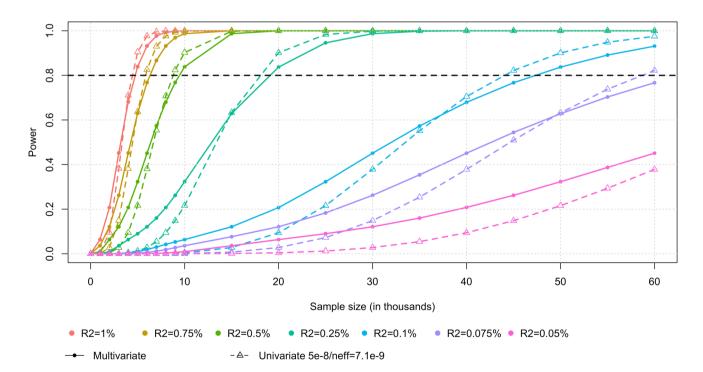


Fig. 5 Statistical power as a function of sample size for multivariate (plain lines) and univariate (dashed lines) GWAS on hippocampus subfields. For all effect sizes and sample sizes, the multivariate approach confers greater statistical power than univariate approach.

Multivariate power presented here corresponds to the varianceweighted power of genetic factors. Averaging the power across factors suggested a possible increase of power (Supplementary Fig. 3, Fig. 6)



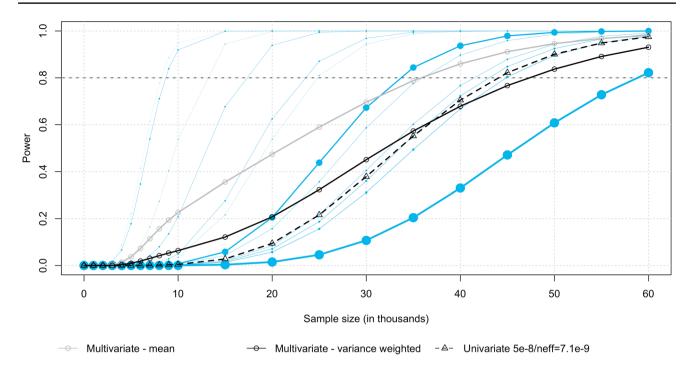


Fig. 6 Power of each genetic factor $(R^2 = 0.001)$ for a multivariate GWAS of hippocampal subfield volumes. The power for each genetic factor is represented in blue. For comparison, we plotted the univariate power (controlling for multiple testing) in black (triangles), the multivariate MANOVA power assuming that all factors are as likely

to exhibit a SNP effect (grey line), the MANOVA power weighting factors by the total phenotypic variance they explain (black line, circles). See Supplementary Fig. 5 for a brief comparison of the SNP effect from each additive genetic factor

the conclusions of this study. In addition, varying the order of the variables in the OpenMx modelling did not change the power estimation (Supplementary Figs. 8, 9).

We confirmed that our analytical derivations were correct by comparing the MANOVA power to those obtained through simulations (Supplementary Figs. 10, 11, 12). We further confirmed that reducing the MANOVA dimension to one phenotype yielded the same statistical power as of a univariate model (Supplementary Fig. 13).

As expected, relying on simulation to estimate statistical power was more time consuming. For our seven subcortical volumes it took 0.47 s to calculate one power curve analytically versus 21 min using simulations. For the twelve hippocampal subfields, the difference was even greater: 0.83 s analytically versus 1 h 2 min using simulations.

Discussion and conclusions

Here, we describe a method to calculate multivariate power of GWAS of real-case scenarios using the outputs from a multivariate twin modelling. Our approach is fast (less than a second), accurate (Supplementary Figs. 10, 11, 12) and computationally economical, as it does not rely on simulation but on analytical power calculation using the F-approximation (Muller and Peterson 1984). Thus, we

could efficiently estimate the power of very large GWAS studies (N = 60,000+), which are realistic sample sizes in the field of imaging genetics nowadays. Our method provides a power estimate that corresponds to the multivariate test implemented in PLINK (Ferreira and Purcell 2009; Purcell et al. 2007) and which is equivalent to the one used in GEMMA (Zhou and Stephens 2014) (when working on related participants) (O'Reilly et al. 2012; van der Sluis et al. 2013; Galesloot et al. 2014).

Using this method, we showed that performing a multivariate GWAS of the volumes for both the subcortical structures and hippocampal subfields confers overall similar power to the standard univariate approach. However, the statistical power may vary greatly depending on the additive genetic source of variance considered (Fig. 6, Supplementary Figs. 2, 4). For example, in both scenarios, the multivariate power was the lowest for SNPs associated with the first additive genetic factor (that contributes to all phenotypes), consistent with previous bivariate simulations (Stephens 2013). For the hippocampal subfields, multivariate GWAS may boost power of detecting SNPs associated with specific subsets of phenotypes (Fig. 6, Supplementary Fig. 5). Indeed, eight additive genetic factors (accounting for 44% of the total additive genetic variance) showed greater power than the univariate approach while four returned similar or lower power. For each additive genetic factor, we



have described the SNP effects on the hippocampus subfields (Supplementary Fig. 6) but more work is needed to understand where the increase/decrease of power comes from. Thus, if overall MANOVA and univariate show similar statistical power, they could lead to the discovery of different genetic variants.

Our results are limited to the two scenarios considered and it would be of interest to extend our analyses, for example considering left and right volumes (instead of the average between left and right), cortical, or voxel-wise measurements. We have released the code used in this analysis to all researchers interested (https://baptistecd.github.io/Power MultivariateGWAS/). It may be applied to variables and scenarios outside the field of brain imaging.

There are some limitations to this study, the main one being that the power calculation relies on estimated parameters (standardised path coefficients from twin modelling). However, we showed that the uncertainty around path coefficients resulted in limited variability in the power calculation, and did not change the conclusions of the analysis (Supplementary Figs. 6, 7). In absence of twin data, path coefficients may be derived from matrices of genetic correlations estimated from SNPs as well as phenotypic correlations. Another limitation concerns the stability of our results when using a different twin sample, possibly with different demographic characteristics. We did not have the data to investigate this limitation. Furthermore, our conclusions are limited to the MANOVA GWAS and there may be another competing multivariate approach that could yield greater power. We recommend to the interested readers the simulation framework of Porter and O'Reilly (Porter and O'Reilly 2017), that allows comparing the power across the different multivariate tests.

More generally, there are a few caveats when performing multivariate GWAS. Firstly, the effect of the SNP is not specific to one variable but rather the set of variables considered. Thus, the discovery analysis would identify SNPs associated with hippocampal volume in general, without testing which subfields the SNP has an effect on. This could be overcome by performing univariate GWAS follow-ups of the multivariate hits to more accurately identify the location of the SNP effect. Another potential consideration is the computing time of multivariate models, compared to univariate ones. Simulation reveals that multivariate GWAS using PLINK would be faster than running sequentially multiple univariate GWAS [see Supplementary Table 3 in (Porter and O'Reilly 2017)]. For multivariate GWAS using mixed models, GEMMA is currently a viable approach for analyses limited to 50,000 participants and ~ 10 phenotypes (Zhou and Stephens 2014). Both programs require little to no reformatting of the data, compared to univariate analyses.

To conclude, more work is needed to identify multivariate GWAS scenarios in imaging genetics that would yield

greater power than standard univariate analyses. Our code allows to efficiently calculate such multivariate power, thus to quickly evaluate new scenarios without time and resource consuming simulations.

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Compliance with ethical standards

Conflict of interest The authors declare that they have no conflict of interest.

Informed consent Written informed consent was obtained from all participants including a parent or guardian for those aged less than 18 years.

Research involving human and animal rights The QTIM study was approved by the ethics review boards of the Queensland Institute of Medical Research, the University of Queensland, and Uniting Health Care, Wesley Hospital, Brisbane. QTIM participants received an honorarium in appreciation of their time. All procedures performed in studies involving human participants were in accordance with the ethical standards of the institutional and/or national research committee and with the 1964 Helsinki declaration and its later amendments or comparable ethical standards.

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